

1 Running Head: Classification Error & LPI error

2

3 Map misclassification can cause large errors in landscape pattern indices:

4 Examples from habitat fragmentation

5

6

7 William T. Langford¹, Sarah E. Gergel², Thomas G. Dietterich³, Warren Cohen⁴

8

9 ¹ corresponding author - National Center for Ecological Analysis and Synthesis, 735 State St.,
10 Suite 300, Santa Barbara, CA, USA 93101, Phone (805) 892-2522, Fax (805) 892-2510

11

12 ² Centre for Applied Conservation Research, Department of Forest Sciences, 3008 – 2424 Main
13 Mall, University of British Columbia, Vancouver, BC, Canada V6T 1Z4

14

15 ³ Computer Science Department, Oregon State University, Corvallis OR 97331, tgd@cs.orst.edu

16

17 ⁴ USDA Forest Service, Pacific Northwest Research Station, Corvallis OR 97331,

18 Warren.Cohen@orst.edu

19

20

April 13, 2005

21

22

REVISED SUBMISSION TO ECOSYSTEMS

ABSTRACT

1
2 Although habitat fragmentation is one of the greatest threats to biodiversity world-wide, virtually
3 no attention has been given to the quantification of error in fragmentation statistics. Landscape
4 pattern indices (LPIs) such as mean patch size and number of patches are routinely used to
5 quantify fragmentation and are often calculated using remote sensing imagery that has been
6 classified into different land cover classes. No classified map is ever completely correct, so we
7 asked if different maps with similar misclassification rates could result in widely different errors
8 in pattern indices. We simulated landscapes with varying proportions of habitat and clumpiness
9 (auto-correlation) and then simulated classification errors on these same maps. We simulated
10 higher misclassification at patch edges (as is often observed), and then used a ‘smoothing’
11 algorithm routinely used on images to correct ‘salt-and-pepper’ classification error. We
12 determined how well classification errors (and smoothing) corresponded to errors seen in four
13 pattern indices. Maps with low misclassification rates often yielded errors in LPIs of much larger
14 magnitude and substantial variability. While smoothing usually improved classification error, it
15 sometimes increased LPI error and reversed the direction of error in LPIs introduced by
16 misclassification. Our results show that classification error is not always a good predictor of
17 errors in LPIs, and some types of image post-processing (e.g., smoothing) might result in
18 underestimation of habitat fragmentation. Furthermore, our results suggest that there is potential
19 for large errors in nearly every landscape pattern analysis ever published, as virtually none
20 quantify the errors in LPIs themselves.

21

22 Key words: fragmentation; landscape metrics; landscape pattern indices; spatial error;
23 classification error; thematic map; accuracy assessment; remote sensing; uncertainty.

INTRODUCTION

1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23

Habitat fragmentation is thought to have significant effects on community structure and composition and to be one of the greatest threats to biodiversity (Villard et al. 1999, Terborgh et al. 2001, Benitez-Malvido and Martinez-Ramos 2003, Cordeiro and Howe 2003, Ferraz et al. 2003). Effects of increasing fragmentation can come from an increase in the number of patches, the distance between patches (Saunders et al. 1991), and the amount of edge habitat within each patch (Brittingham and Temple 1983; Andr n and Angelstam 1988, Laurance et al. 2000). Landscape fragmentation is commonly characterized using measures of these and other values such as mean patch size. Because software to compute these landscape pattern indices (LPIs) is widely available, pattern analyses are routinely performed for a variety of habitats and for many different purposes ranging from habitat conservation to regional planning (Cardille and Turner 2001, Turner et al. 2001, McGarigal et al. 2002, Fahrig 2003).

LPIs are often computed over remote sensing images that have been classified into different land cover classes (Skole and Tucker 1993, Peralta and Mather 2000, Griffiths et al. 2000, Imbernon and Branthomme 2001), but there are always errors made in classifying the pixels of an image into land cover classes. This lack of accuracy raises the question of whether these classification errors could lead to substantial errors and variation in the LPIs derived from classified maps (Hess 1994). Despite its apparent importance, virtually no study measures the error in LPIs, much less accounts for the error caused by image misclassification. This oversight may have serious consequences for both science and policy because there is potential for errors of unknown magnitude in nearly every landscape pattern analysis ever derived from classified images.

While a great deal of effort has gone into techniques for assessing classification accuracy

1 (Congalton and Green 1999, Stehman 2001), it is generally specified in terms of the
2 percentages of misclassified pixels, with no reference to the location of the errors. However,
3 higher classification errors are often associated with textured areas or patch boundaries (Edwards
4 and Lowell 1996, Plourde and Congalton 2003). While several authors have examined other
5 causes of error in LPIs (Turner et al. 1989, Cardille and Turner 2001, Saura and Martinez-Millan
6 2001), the effect of classification errors on LPIs has rarely been addressed directly. When it has
7 been addressed (Hess and Bay 1997, Wickham et al. 1997, Brown et al. 2000, Shao et al. 2001),
8 differing conclusions have been reached. The conflicting conclusions may be partially due to the
9 fact that each of these studies was based on a single image or landscape, and thus did not control
10 for the impact of landscape structure.

11 *Objective*

12 Here, we use a series of simulated landscapes and classification errors to test the notion that LPI
13 error is necessarily correlated with classification error. Specifically, we address the following
14 two questions:

15 *1) How do image classification errors and levels of smoothing affect LPIs of fragmentation?*

16 *2) How do the amount of habitat and its clumpiness affect the error in the LPIs?*

17 Unlike previous work, these simulations allow us to examine both the magnitude and
18 spread in LPI error among landscapes that are strictly controlled for spatial characteristics that
19 might affect the values of the LPIs. While our simulated landscapes and classification errors
20 have elements of real applications to them, it is important to note that we do not claim to build a
21 predictive model of the precise amount of expected LPI error for any particular classified map.

22 **METHODS**

23 *Overview*

1 We created a set of 10,800 simulated landscapes designed to represent specific aspects of the
2 variability seen in real landscapes, as well as aspects of the remote sensing image classification
3 process. We first created 270 simulated ‘correct’ base landscapes with two land cover classes:
4 habitat and background. These ‘correct’ base maps represented images where every pixel has
5 been classified as either habitat or background with no error. These maps were designed to vary
6 systematically in the proportion and clumpiness of habitat. We also created ‘incorrect’
7 misclassified maps from the correct base maps, representing images that have been incorrectly
8 classified to some degree, mimicking two types of common classification errors. We ‘smoothed’
9 the images using a process routinely applied to correct salt-and-pepper errors on images.
10 Afterwards, we determined the impact of classification errors and smoothing on several LPIs
11 derived from the simulated maps. Finally, we determined whether classification errors were
12 related to the magnitude of and spread in LPI error.

13 *Measuring Classification Error*

14 We refer to two commonly used measures of classification error: producer’s error and user’s
15 error, both measured on a per class basis, as opposed to the total error for all habitat or land
16 cover classes. We chose these measures of classification error because nearly all current research
17 reports classification errors in this way. The producer’s error (e_p) is the probability that a true
18 land cover class will be incorrectly mapped and measures the errors of omission. It represents the
19 classification errors that we systematically induced in our maps. In our study with two cover
20 types, producer’s error refers to the percentage of habitat pixels in the “correct” map that are
21 incorrectly labeled in the “misclassified” map (i.e., are labeled as background):

$$22 \quad e_p = \text{fn}/(\text{tp}+\text{fn}) \quad (1)$$

23 where fn=false negatives, tp=true positives and we treat “habitat” as the positive class.

1 landscapes simulated by RULE and much theoretical work in habitat connectivity is based on
2 landscapes generated using this software (With and King 1997), thus further enhancing the utility
3 of our results.

4 We varied the proportion of the landscapes occupied by habitat from ten to ninety percent
5 of the landscape in ten percent increments so that we could examine the impact of habitat loss on
6 LPIs. In addition, we varied the Hurst exponent, H , which ranges from 0 to 1 to examine the
7 impact of the clumpiness of fragmentation on our results. A Hurst exponent of 0 represents
8 landscapes that are negatively auto-correlated and an exponent of 1 represents landscapes that
9 are extremely positively auto-correlated. We examined H levels of 0.2, 0.5, and 0.8. Thus, we
10 created 9 proportions of habitat and 3 levels of auto-correlation, with 10 replicates of each, for a
11 total of 270 initial correct base maps. While this does not mimic every possible aspect of
12 landscape structure, varying these two simple parameters created a wide range of landscape
13 structure (Figure 1).

14 *Incorrect and Smoothed Maps.* We created ‘incorrect’ maps from ‘correct’ maps to mimic two
15 types of classification error: (a) randomly located misclassification (“salt and pepper” error); and
16 (b) increased misclassification near patch boundaries (as compared to the interior of patches).
17 While this is not the only error model possible, random error and edge error are a part of any
18 classifier's error. Moreover, this error model creates errors that may directly influence
19 fragmentation through the generation of spurious patches. It also matches the error model used in
20 Wickham et al. (1997). This was important for our study because we wanted to examine whether
21 the same error model would lead to different conclusions on different landscapes. Other error
22 models, for example, ones with more spatial autocorrelation are left for future studies.

23 Because our maps contained only two classes, we induced errors in the classification of

1 individual pixels on the correct map by simply changing habitat cells to background, or vice
2 versa, with a given probability (or error rate). This type of error is routinely termed ‘producer’s
3 error.’ We assumed that error rates near patch edges were 10% higher than in patch interiors
4 (e.g., due to mixed pixels, Wickham et al. 1997). For inducing errors, we defined an edge pixel
5 as any pixel with at least one of its four neighbors belonging to the other category. Thus, we set
6 the error rates in the patch interiors at 10% with corresponding edge error rates of 20%. We
7 created 10 incorrect maps from each correct base map, resulting in 2700 total incorrect maps.

8 We then removed small, isolated regions assumed to be in error by applying a smoothing
9 technique that removes all regions smaller than the size of a designated minimum mapping unit
10 (MMU). Any patch smaller than the size of the minimum mapping unit is removed by changing
11 the classification of its pixels to the classification of the patch with which it shares the longest
12 border. In the case of only two classes, that border is always with a fully surrounding patch. We
13 employed minimum mapping units of 2, 4 and 9 cells to remove all patches below these size
14 thresholds, for a total of 8100 smoothed maps. We chose this method rather than a majority filter
15 because it is simple to implement and because a majority filter tends to remove edge complexity.
16 The sizes were chosen to roughly correspond to a graduated set of patch sizes: a pair of adjacent
17 pixels, a 2x2 square, and a 3x3 square. Similar procedures were used in the classified
18 WISCLAND Land Cover data set, where upland land cover categories (excluding URBAN)
19 were ‘smoothed’ to patches no smaller than four contiguous pixels using a clump-sieve-fill
20 algorithm, whereas wetlands were smoothed using a minimum mapping unit of two pixels
21 (WISCLAND 1993). Brown et al. (2000) used sieves of size 1, 3, and 10 hectares as well as
22 majority filters of sizes 3x3 and 5x5.

23 *Conservative classification errors.* It is unlikely that our simulated errors overestimated

1 classification error rates found in real maps at edges or patch interiors. Reported classification
2 error rates for some commonly studied data sets vary widely depending on land cover class, level
3 of classification and method of accuracy assessment. For example, in the 1992 U.S. National
4 Land-Cover Dataset where accuracy assessment was done extensively and carefully, per class
5 user's accuracies for Anderson Level I classifications for the mid-Atlantic region range from
6 35% correct to 92% (Stehman et al. 2003). Values for Anderson Level II classifications for the
7 same region range from 1% to 92%. There is also evidence for optimistic bias in the reporting of
8 classification error in many studies (Hammond and Verbyla 1996, Stehman 2001). For the
9 purposes of simulating edge-biased classification error, we have assumed patch edges to be one
10 pixel wide (Wickham et al. 1997). However, true edge widths may be larger in many landscapes
11 (Edwards and Lowell 1996), especially in heavily textured images. Thus, our edge width of one
12 pixel is likely to lead to conservative edge errors.

13 *Measuring Fragmentation*

14 We applied Fragstats 3.0 (McGarigal et al. 2002) to calculate the following LPIs on simulated
15 correct, incorrect, and smoothed landscapes: a) Mean Shape Index, b) Total Edge (m), c)
16 Number of Patches, and d) Mean Patch Size (ha). (Details on the LPIs calculated by Fragstats
17 can be found in the Fragstats documentation at:
18 <http://www.umass.edu/landeco/research/fragstats/fragstats.html>). Increasing values of mean
19 patch size indicate less fragmentation, whereas increases in the other LPIs are indicative of
20 greater fragmentation. We make no claims about whether these are ecologically informative
21 measures of fragmentation. Rather, we chose these LPIs because they are among the simplest to
22 understand and the most widely employed measures for quantifying habitat fragmentation. They
23 were also hypothesized to be among the most affected by edge misclassification.

Analysis of Results

For simplicity, we considered only binary maps (with only two land cover classes) and only examined the results for one class. Although real maps may have more than one class, the LPIs of fragmentation we examined are calculated on a ‘per class’ basis (e.g., for one habitat type only, assuming all other habitat types are background). As long as the LPI of interest does not distinguish among the different classes that make up the background class, the value of the LPI will be identical in the multi-class and the combined binary versions of the map.

It is also very important to examine classification error on a per class basis rather than computing total classification error for the landscape as a whole because a classifier can have low accuracy for one class of interest, but still have high overall accuracy when averaged across all classes. For example, the total classification error can be small and misleading when a map has low classification errors for abundant classes, and high classification errors for less abundant classes. Thus, examining classification error and LPI error both on a ‘per class’ basis makes the most sense for this study.

For each LPI on the incorrect and smoothed landscapes, we determined the percent error in the LPI relative to the correct landscape, which we termed % LPI Error.

$$\% \text{ LPI Error} = ((\text{LPI}_{\text{incorrect}} - \text{LPI}_{\text{correct}}) / \text{LPI}_{\text{correct}}) * 100 \quad (3)$$

We plotted % LPI Error versus User's Error for the initial misclassifications as well as for each level of smoothing at different minimum mapping units. While we demonstrate the spread in LPI error within each user's error value quite clearly using these graphs, we do not compute a standard deviation or variance of LPI errors. This would require arbitrarily binning data points (by base landscape, proportion, clumpiness, or user's error, etc.) when our purpose is simply to examine whether for any given user's error, there is a large spread of values of LPI error.

RESULTS

1
2 First, we summarize the general behavior of our landscape model and error model by examining
3 the relationship between producer's error (which we manipulated) and the resulting user's error.
4 Second, we examine the impact of the classification errors on the computed LPIs to determine if
5 smoothing affected LPI error. We discuss the results for each LPI in detail. Lastly, we examine
6 the relative impact of landscape structure (clumpiness and habitat loss) on LPI error.

7 To fully understand our results, it is important to explain how our error model and our
8 landscape model are related (Figure 2). Even though our simulated producer's errors in habitat
9 classification were limited to 10 – 20%, it resulted in a larger range of user's errors, between 0
10 and 60% (Figure 3). User's errors were generally higher in the incorrect landscapes (before
11 smoothing) with low proportions of habitat (Figure 3). However, ‘smoothing’ of an image
12 reduced maximum user's error by roughly half, from around 50% in the incorrect images to less
13 than approximately 25% when smoothed (MMU=9) (Figure 3). We have shown the full range of
14 values for user's and producer's error in Figure 3 to show the effects of smoothing on those
15 errors. In Figures 4 and 5 though, we have only shown values for images where both user's and
16 producer's error are less than or equal to 15%. While we computed results for all of the simulated
17 landscapes that we generated, we have chosen to only show results here for maps with the most
18 conservative amounts of classification error. Even though classification rates are often higher
19 than 15% and our LPI errors for those classification error rates were even more extreme, we have
20 done this so that we are certain not to display results for classification error rates that any users
21 would reject as being too high to use in a real application.

22
23 *How do image classification errors and levels of smoothing affect LPIs of fragmentation?*

1 Classification errors often resulted in large errors in LPIs, even at classification error rates
2 considered low by the remote sensing community. While the relationship between the values of
3 LPIs on the correct versus the incorrect and smoothed maps was roughly linear for Total Edge
4 (Figure 4e-h), it was not for the other LPIs. For the Number of Patches, the relationship between
5 the correct and incorrect values depends on the minimum mapping unit (MMU) used for
6 smoothing. It was linear only for MMU=4 and 9. When examining percent error in LPIs relative
7 to the correct image, the errors in LPIs were extremely high (Figure 5), in a number of cases,
8 higher than 1000% (Figures 5e,f,i,j,p). User's error did not reliably correspond to LPI error for
9 any LPI examined, and therefore, it was not a useful predictor of LPI error. Smoothing did not
10 consistently reduce the magnitude of errors in LPIs relative to the original correct classification.
11 However, smoothing using MMU=9 always reversed the direction of error caused by the initial
12 misclassification (overestimation changes to underestimation and vice versa) for all the LPIs
13 examined (Figure 5). Thus, while smoothing to remove salt and pepper error improved per class
14 user's error, it sometimes increased LPI error (Figure 5). We next examine each LPI in greater
15 detail.

16 LPI errors for Mean Shape Index were generally less than $\pm 10\%$ in the incorrect
17 landscapes (Figure 5a), but increased to 50% with smoothing (Figure 5b-d). The errors were not
18 consistently biased in one direction, as the LPI was underestimated for the incorrect landscapes
19 (5a), but overestimated for the MMU=4 (5c) and 9 landscapes (5d). However, the lower user's
20 errors in the smoothed landscapes still yielded both higher magnitude and greater spread in LPI
21 error within a given user's error (Figure 5d).

22 For Total Edge, the maximum percentage LPI error approached 4000% (Figure 5e).
23 Smoothing reduced the LPI error to the range between +150% and -60% (Figure 5g-h), but the

1 direction of error differed depending on the minimum mapping unit. Total Edge was
2 overestimated on the initial incorrect, MMU=2, and MMU=4 landscapes (Figure 5e-g) and
3 underestimated by more than 50% for the most fragmented landscapes when MMU=9.

4 The percent error in the Number of Patches (NP) relative to the correct image ranged
5 from approximately 0 to 10,600%. The behavior of NP was qualitatively similar to that of Total
6 Edge, where the LPI was overestimated for the initial incorrect landscape and for the MMU = 2
7 landscapes (Figure 5i-j), but then underestimated by as much as 100% for MMU=9 (Figure 5l).

8 For Mean Patch Size (MPS), the initial misclassifications resulted in underestimation of
9 the LPI by as much as 100% (Figure 5m). When smoothed using MMU=2, MPS was both over-
10 and under-estimated (Figure 5n). Successive smoothing using MMU=4 and 9 resulted in
11 increases in LPI error, to more than 1000% for MMU=9 (Figure 5p).

12 Our results suggest that the magnitude and spread of LPI errors due to misclassification
13 can be quite large. Moreover, LPI errors do not always decrease with spatial post-processing
14 techniques, such as smoothing, that are routinely applied to reduce user's error. In short, the
15 spatial arrangement of classification error is at least as important as the amount. LPI errors are
16 not always lower on maps with lower user's errors, and maps with the same user's error can
17 frequently result in maps with LPI errors of very different magnitudes.

18

19 *How do the amount of habitat and its clumpiness affect the error in the LPIs?*

20 The magnitude of LPI errors was affected by the structure of the landscape, but it was affected
21 more by the clumpiness (H, the auto-correlation parameter) than by the proportion of habitat.
22 This was especially evident for Total Edge, Number of Patches, and Mean Patch Size before
23 smoothing (Figure 5e.i.m.n). For Total Edge, LPI error was lowest for H=0.2 (dispersed), and

1 much greater when $H=0.8$ (clumpy), approaching 4000% error (Figure 5e). Qualitatively
2 similar patterns were evident for Number of Patches. The effect of landscape clumpiness on error
3 in Mean Patch Size was dependent on MMU. Before smoothing, the smallest LPI errors were
4 roughly -50% in the $H=0.20$ landscapes (Figure 5m), and LPI errors were as large as -100%.
5 When smoothed, the largest LPI errors were in the $H=0.20$ landscapes (Figure 5o-p), and the
6 lowest LPIs errors were in clumped landscapes (with $H=0.80$). While the proportion of habitat
7 had less effect on our LPI error, it is correlated highly with user's error (Figure 3), and thus our
8 results must be seen in that context. The lowest user's errors always occurred in the landscapes
9 with the highest proportion of habitat, but this was often the region where the highest LPI errors
10 occurred.

11 **DISCUSSION**

12 We are aware of only four other studies addressing the effects of classification error on LPI error
13 and all but one of these studies were based on either a single image or landscape and did not
14 control for the impact of landscape structure. The one study that does use more than one
15 landscape and does control for landscape structure is Hess and Bay (1997). Like our study, they
16 examined the effect of map error on several LPIs. Unlike our study, their indices were non-
17 spatial ones, including percent cover and two commonly used diversity indices. They used three
18 levels of map error and found that they did cause error in the measures. They further described a
19 method to put confidence intervals around the measures. Of the remaining three studies, only one
20 measured both accuracy and variability in the LPIs. Wickham et al. (1997) simulated
21 classification errors over portions of a land cover map derived from a single TM image. As in
22 our study, they computed the difference in the values of several LPIs between the original base
23 map and the maps with simulated classification errors. They concluded that for the landscape and

1 methods they used, classification error did not increase LPI error. Instead of simulating errors,
2 Shao et al. (2001) had 23 different interpreters classify a single TM image and then measured the
3 variation in LPIs over the 23 different maps. They found that even though there was not much
4 variation in the accuracy of the classifications, there was a great deal of variation in the LPI
5 error. The third related study is that of Brown et al. (2000) in which they examined estimates of
6 error in pattern indices used for change detection. They classified images for two forested areas,
7 subsetted the two areas into many smaller landscapes and then compared the LPI values obtained
8 in overlapping areas of adjacent images photographed around the same time. They found that the
9 LPIs of mean patch size and number of patches were more error prone than the edge density LPI.

10 Our experiments demonstrate that classification error is not always a reliable predictor of
11 LPI error, and that one cannot assume a map with low classification error will produce accurate
12 LPIs. In our simulated landscapes, the spread in LPI error was generally large, and the magnitude
13 in LPI error was almost always much larger than the magnitude of classification error, even for
14 small classification errors. Also, the common practice of reducing classification error by spatially
15 smoothing a classified map using a minimum mapping unit sometimes increases LPI errors. This
16 result is also consistent with the results in Brown et al. (2000) which is based on empirical data.
17 The consistent underestimation of number of patches and consistent overestimation of total edge
18 and mean patch size in smoothed classifications suggest that landscape fragmentation may be
19 routinely underestimated as a result of smoothing classifications and should be investigated
20 further. Since the landscapes and error models in this paper are artificial, the specific quantitative
21 results obtained here do not generalize to all landscapes and error matrices. However, our results
22 show large and unpredictable amounts of error in LPIs on images with very low classification
23 error by the standards of the remote sensing community. In addition, our results show that

1 different smoothing and/or classification techniques may be recommended for reducing errors
2 in different LPIs even on the same image. In the following sections, we discuss these points in
3 greater detail.

4

5 *How do image classification errors and smoothing techniques affect LPIs of fragmentation?*

6 Our results suggest that the accuracy of LPIs derived from classified images may not be easily
7 predicted from the accuracy of the classification. In our simulated landscapes, the magnitude of
8 LPI error was nearly always a great deal larger than the magnitude of the corresponding
9 classification error, even when classification error was small. While there is no reason to expect
10 that the value of the LPI error should *equal* the value of the classification error, we often found
11 that the errors were not even within the same order of magnitude. Moreover, the large spread in
12 LPI error at all levels of classification error (shown in Figure 5) means that we cannot fit any
13 single function from classification error to LPI error in the conditions that we have simulated.
14 We cannot even guarantee the weak criteria that the rankings of maps by classification error
15 would yield the same results as a ranking based on LPI errors.

16 Predicting LPI error from classification error was further confounded by the fact that the
17 common practice of using minimum mapping units to reduce salt and pepper classification error
18 actually increased LPI error for mean patch shape and mean patch size. Moreover, it always
19 reversed the direction of error (from over to underestimation or vice versa). Further, the ideal
20 smoothing levels for reducing LPI error varied by LPI (Figure 5). For example, the smallest LPI
21 error values and spread for Mean Patch Shape occurred in scenarios with no smoothing, while
22 the best smoothing level for Total Edge was MMU=9; for Number of Patches, MMU=4; and for
23 Mean Patch Size, MMU=2. This suggests that minimizing error for each LPI may require using

1 different maps derived from different classifiers or smoothing levels for each LPI.

2

3 *How do the amount of habitat and its clumpiness affect the error in the LPIs?*

4 The proportion of habitat had less effect on LPI error than habitat clumpiness did. As the
5 smoothing MMU increased, clumpiness had less effect on LPI errors for Mean Patch Shape and
6 Mean Patch Size, but greatly affected LPI errors for Total Edge and Number of Patches. While
7 habitat proportion was not related closely to LPI error in our simulations, it had a large effect on
8 the difference between user's error and producer's error generated by our model. User's errors
9 were generally higher in low proportion landscapes (Figure 3). This error pattern would not be
10 unreasonable to expect using any classifier for several reasons. First, there are likely to be
11 relatively more edge and mixed pixels in lower proportion landscapes, exactly the type of pixels
12 where more classification error is expected. Second, the small sample size of pixels in low
13 proportion landscapes results in fewer training data available for training a classifier. Lastly,
14 higher user's error in low proportion landscapes is likely simply given the equation for User's
15 Error: $fp/(tp+fp)$. In a low proportion landscape, this equation would be dominated by the false
16 positives, given the small number of true positives possible even if 100% of habitat was
17 recognized correctly. In future experiments, we could totally eliminate this effect by writing a
18 more complicated error model that draws pixels in a different way to control for user's error as
19 well. We did not rerun the experiments here with the more complicated model because our
20 conclusions remain the same even if we remove all points with user's error greater than 15%.

21 *Bounds of Generalization* Our primary goals were to characterize a certain type of classification
22 error over a range of landscape structures and to test the hypothesis that a map with small
23 classification error necessarily yields spatially reliable LPIs. Our results should not be

1 generalized quantitatively to all landscapes, all LPIs, or all types of classification error. Our
2 results are limited to the landscape structures, LPIs, smoothing and classification error models
3 tested. In spite of these limitations, we argue that the scenarios we have presented have enough
4 realism to reasonably reflect some of the complexity of a real application, and demonstrate that
5 this complexity can generate subtle and counterintuitive outcomes.

6 Just as we recommend not over-generalizing from our results, our study strongly
7 illustrates the problem in drawing general conclusions based on classifications derived from one
8 original base landscape or image. As an example, even though our experiments employed
9 classification error assumptions similar to those of Wickham et al. (1997), our study yielded
10 much larger errors in LPIs not only because we used different LPIs, but more importantly we
11 used a range of different landscape structures.

12 *Simulations vs. Real Landscapes* The danger of over-generalizing from a single map is made
13 particularly clear by the use of multiple simulated landscape maps that we have presented here.
14 Simulated landscapes are often employed to directly control, manipulate, and replicate features
15 of landscape structure (Gardner et al. 1987, Gardner et al. 1991) such as the proportion of habitat
16 types or clumpiness (With and King 1997, Turner et al. 2001, Gergel 2002). Controlling for the
17 variability in real landscapes is extremely problematic because they vary widely in many of these
18 features that influence the behavior of LPIs. Often, they are also highly anisotropic and non-
19 stationary (containing different gradients of clumpiness or auto-correlation, and in different
20 directions). This makes their patterns uneven within one landscape. Thus, any subset of real
21 landscape imagery used for a study such as this is unlikely to systematically span the range of
22 proportions or variability in auto-correlation. Furthermore, the proportions of different habitat
23 types on a remote-sensed image are ultimately dependent on the spatial resolution and on the

1 level of thematic resolution of land cover classes chosen to create the map (e.g., 3 vs. 5 cover
2 types).

3 Equally important is that when using a classified image as the ‘correct’ base landscape
4 for simulating classification errors, the ‘correct’ patch boundaries and LPI values cannot be
5 known due to LPI errors already introduced by the classifier. The range of LPI values on the
6 initial correct map (if obtained this way) would incorporate the classifier's bias and need not
7 represent the true range of LPI values. For example, smoothing tends to reduce the complexity of
8 patch edges and the number of small patches.

9 We argue that until we understand the behavior of LPIs in highly controlled and
10 replicated scenarios, we cannot expect to understand or predict their behavior on real maps
11 which vary in many uncontrolled ways. The numerous sources of error and variability make it
12 difficult to isolate the factors influencing the behavior of LPIs on real landscapes or those from
13 any classified image. With simulated landscapes, we can systematically vary proportion and
14 spatial autocorrelation and we can generate multiple realizations of these landscapes using the
15 same parameters.

16 *Error models.* One limitation in our error model is that spatial structuring of error is not directly
17 accounted for beyond edge effects. Directly modeling spatial autocorrelation in the errors might
18 have different results and should be investigated since many errors in our model come from the
19 splitting off of small patches. However, there are several factors that suggest that results derived
20 from this model are still of interest. First, our experiments showing smoothing with a minimum
21 mapping unit of 9 cells do address a certain amount of autocorrelation because there is spatial
22 grouping of errors when no patch can be smaller than 9 cells. Second, as the spatial resolution of
23 imagery used increases, there is less averaging of the signal; consequently, the local

1 characteristics of the image are less uniform. Per pixel classifiers that do not take this texture
2 into account are more likely to generate varying classifications of neighboring pixels. These
3 classifications are likely to require post-classification smoothing similar to that employed in our
4 simulations, possibly with similar results. Third, the amount of salt and pepper error that occurs
5 in a classified image is partly a function of the skill of the operator. The experiments in Shao et
6 al. (2001) with multiple operators showed many different outcomes even given exactly the same
7 input. Anyone with access to an image processing program can push a button to classify an
8 image and then compute LPIs on that output. Users whose primary expertise is not in image
9 processing, may have little idea how to deal with issues such as texture in an image and produce
10 speckled classifications which they may or may not smooth afterwards. In either case, their
11 errors may be qualitatively similar to those expressed in our error model. Finally, our results
12 have shown that even if there is less than 1 or 2% error of this kind, it can still generate huge
13 amounts of error in some LPIs (e.g., see Figure 5p).

14 *Normalization of LPI errors for comparison* Another important issue is that the ability to
15 compare and rank different LPIs by error requires a fair method for normalizing LPI errors.
16 Throughout this paper we have examined LPI error as a percentage of the correct LPI value, but
17 the total *possible* percent error can differ greatly among LPIs. When the range of an LPI is
18 infinite or allows values to become infinitesimally small (i.e., arbitrarily close to zero), there
19 will be no upper bound on the percentage error possible. In contrast, any LPI whose magnitude is
20 bounded above and below and does not include any neighborhood of zero will have bounds on
21 the percentage error it can possibly attain. It may thus appear better (lower error) than an LPI
22 with errors that can be unbounded. For example, the fractal dimension of a planar region can
23 only vary between 1 and 2. Consequently, it can never have an error greater than 100% because

1 the denominator can never be less than one and the numerator can never be greater than one.
2 Similarly, an LPI may be *effectively* bounded if it is very difficult or uncommon to observe
3 values outside a narrow range (e.g., the Shape Index in our studies). In either case (actual or
4 effective bounding of error), it is inappropriate to directly compare the magnitude and variation
5 of the error of bounded LPIs with unbounded ones. The bounded LPI may appear to have very
6 little percentage error, but this may be simply because its range is so small that the ecologically
7 relevant distinctions in the LPI's values require high precision that is irrelevant in the unbounded
8 LPI.

9 One way to normalize the errors would be to normalize them against what is considered
10 to be the smallest ecologically relevant distinction in the application of interest. For general
11 comparison of LPIs however, it would be useful to have a normalization method that was more
12 independent of specific applications. One way to do this would be to compare the errors to the
13 largest error "reasonably possible" for that LPI. For example, we could assume that a classifier
14 should not do any worse than randomly guessing classifications. More research is necessary to
15 determine what are the appropriate characteristics and candidates for a normalization method to
16 allow comparison of LPI errors. However, it is clear that any future studies that attempt to *rank*
17 LPIs in terms of LPI error will need to normalize their error measures in some way so that the
18 results are meaningful.

19 *Accuracy Assessment* Our work suggests that both the creators and the users of classified images
20 need to do more to measure spatial aspects of classification errors in maps. In particular, better
21 techniques for accuracy assessment of LPIs need to be developed for several reasons. First, as we
22 have shown, non-spatial measures of accuracy (user's error) do not necessarily correspond to
23 errors in spatially-explicit LPIs. To date, studies that do measure spatial aspects of classification

1 error (Foody 2002, Hagen 2003, Pontius et al. 2004), do not examine how those error
2 measures relate to the errors in the LPIs. Second, many users of classified remote sensing
3 imagery are often unlikely or unable to verify the spatial accuracy of classifications themselves
4 due to budget or expertise or because not all of the original reference data is available to the user
5 (e.g., because of agreements with land owners covered by the map). In such cases, the producers
6 of classified imagery would help their users by evaluating spatial characteristics of classification
7 error instead of just counting misclassified pixels.

8 However, it is not clear whether it is possible to develop predictive models of LPI error
9 that can be generalized to real-world applications. The reason for this is that the pattern of errors
10 in any classified map is the result of complex interactions among many factors. These factors
11 include the classification algorithm, its training data, the user's skill, the landscape, the class
12 structure (e.g., relative abundance of classes, relative importance of different types of errors,
13 patch shapes, patch interlacing, anisotropy) as well as the spatial distribution of classification
14 errors (e.g., location of easily confused classes relative to each other). It may be more useful to
15 develop project-specific predictive models for LPI error based on image characteristics, as
16 Brown et al. (2000) did for change detection in LPIs in forest cover maps. At a minimum
17 however, analogous to classification error analysis, subsamples of the images of interest should
18 have patch boundaries identified through some more reliable method of assessment. These
19 subsamples could then be used to provide a standard for assessing the correctness of spatial
20 measures derived from their classification.

21 In this paper, we do not mean to suggest that deriving a more accurate value of the LPI as
22 defined for the given single landscape will solve all problems with LPIs. Even if we could
23 identify the correct value of an LPI from a classified map, there are other issues about whether

1 further accuracy assessment in light of the results presented here. Errors in LPIs for all habitat
2 types deserve further consideration, particularly as remote sensing data becomes available at ever
3 increasing levels of resolution. Such imagery provides an unprecedented opportunity to quantify
4 and monitor all habitats, but especially, smaller habitats such as ephemeral wetlands and narrow,
5 linear riparian zones which are often missed in routine mapping using coarser scale data sources.
6 The linear nature of riparian habitats might render them particularly sensitive to errors in
7 classification – as a misclassified pixel or two could shatter one long contiguous patch into
8 several smaller patches. While presenting valuable new sources of data at the resolutions needed
9 for many ecological applications, spatial measures derived from classifications of such data
10 sources must be used with care. A recent review of papers on habitat fragmentation discussed the
11 challenges in discriminating the impact of habitat loss from that of habitat fragmentation on
12 biodiversity, and found that the impact of fragmentation was weaker and less consistent than that
13 of habitat loss (Fahrig 2003). This conclusion is interesting in light of the fact that errors in
14 measuring habitat *loss* are routinely quantified (via classification errors), whereas errors in
15 measuring landscape *pattern* are generally not quantified, and may be substantial. The kinds of
16 errors found in LPIs in our study suggest there may be some danger that fragmentation may be
17 routinely underestimated as a result of smoothing and we recommend this possibility be
18 investigated further.

19 In summary, our work shows that the spatial arrangement of classification errors affects
20 the amount of error in LPIs. Classification errors often resulted in large errors in LPIs, even at
21 classification error rates considered low by the remote sensing community. The amount of map
22 classification error is not necessarily a reliable predictor of LPI error. One cannot assume that a
23 map with low classification error will produce relatively accurate LPIs. This suggests that the

1 results of any fragmentation study where LPI errors have not been measured may be incorrect,
2 and potentially to a large degree. No one would classify an image and then claim that the
3 classifications were accurate without testing that claim, yet virtually no study using LPIs derived
4 from a classified image actually measures the accuracy of the LPIs derived from those maps.
5 More emphasis must be placed on evaluating the sources and spatial nature of error in land cover
6 data used for conservation purposes, because over- or under-estimation of the degree of
7 fragmentation can have significant impacts on both public policy and scientific conclusions
8 related to habitat fragmentation. Simply saying that it is difficult or expensive to measure LPI
9 accuracy will not correct erroneous conclusions derived from faulty LPI values.

10 **ACKNOWLEDGEMENTS**

11 The authors thank D. Brown, J. Cardille, Y. Carmel, M-J. Fortin, G. Hess, M. Kinnaird, C.
12 McCain, J. Parrish, K. Phrodite, V. Radeloff, and D. Vazquez for valuable comments on this
13 paper. We also thank an anonymous reviewer of an earlier version of this paper for comments on
14 normalization methods. W.T.L. was supported by NSF grants IRI-9204129, IRI-9626584, ITR-
15 0085836, ONR grant number N00014-95-1-0557, AFOSR grant number F49620-98-1-0375, the
16 NASA Terrestrial Ecology Program, EPA STAR fellowship number U 915196-01-1. Part of this
17 work was conducted while W.T.L. and S.E.G. were Postdoctoral Associates at the National
18 Center for Ecological Analysis and Synthesis, a Center funded by NSF (Grant #DEB-0072909),
19 the University of California, and the Santa Barbara campus.

20 **LITERATURE CITED**

21 Andrén, H. and P. Angelstam. 1988. Elevated predation rates as an edge effects in habitat
22 islands: experimental evidence. *Ecology* 69:544-547.
23 Benitez-Malvido, J. and M. Martinez-Ramos. 2003. Impact of forest fragmentation on understory

- 1 plant species richness in Amazonia. *Conservation Biology* **17**: 389-400.
- 2 Brown, D. G., J. Duh, and S. A. Drzyzga. 2000. Estimating error in an analysis of forest
3 fragmentation change using North American landscape characterization (NALC) Data.
4 *Remote Sensing of Environment* **71**:106-117.
- 5 Brittingham, M.C. and S. A. Temple 1983. Have cowbirds caused forest songbirds to decline?
6 *Bioscience* 33:31-35.
- 7 Cardille, J.A. and M.G. Turner. 2001. Understanding landscape metrics I. Pages 85-100 in
8 *Learning Landscape Ecology: A Practical Guide to Concepts and Techniques*. S.E.
9 Gergel and M.G. Turner, editors. Springer-Verlag, New York, New York, USA.
- 10 Congalton, R.G., and K. Green. 1999. *Assessing the Accuracy of Remotely Sensed Data:*
11 *Principles and Practices*. Lewis Publishers, Boca Raton, Florida, USA.
- 12 Cordeiro, N. J. and H. F. Howe. 2003. Forest fragmentation severs mutualism between seed
13 dispersers and an endemic African tree. *PNAS* **100**: 14052-14056.
- 14 Edwards, G., and K. E. Lowell. 1996. Modeling Uncertainty in Photointerpreted Boundaries.
15 *Photogrammetric Engineering and Remote Sensing* **62**:377-391.
- 16 Fahrig, L. 2003. Effects of habitat fragmentation on biodiversity. *Annual Review of Ecology*
17 *Evolution and Systematics* **34**:487-515.
- 18 Ferraz, G. et al. 2003. Rates of species loss from Amazonian forest fragments. *PNAS* **100**:
19 14069-14073.
- 20 Foody, G. 2002. Status of land cover classification accuracy assessment. *Remote Sensing of*
21 *Environment* **80**: 185-201.
- 22 Fortin, M. J., B. Boots, F. Csillag, and T.K. Rempel. 2003. On the role of spatial stochastic
23 models in understanding landscape indices in ecology. *Oikos* **102**: 203-212.

- 1 Gardner, R.H. 1999. RULE: map generation and spatial analysis program. Pages 280-303 in
2 J.M. Klopatek and R.H. Gardner, editors. *Landscape Ecological Analysis: Issues and*
3 *Applications*. Springer-Verlag, New York, New York, USA.
- 4 Gardner, R. H., B. T. Milne, R. V. O'Neill, and M. G. Turner. 1987. Neutral models for the
5 analysis of broad-scale landscape patterns. *Ecosystems* **1**:19-28.
- 6 Gardner, R. H., and R. V. O'Neill. 1991. The use of neutral models for landscape analysis. Pages
7 289-307 in M. G. Turner and R. H. Gardner, editors. *Quantitative Methods in Landscape*
8 *Ecology: The Analysis and Interpretation of Landscape Heterogeneity*. Springer-Verlag,
9 New York, New York, USA.
- 10 Gergel, S.E. 2002. Cumulative impact of levees and dams on the duration of temporary
11 floodplain ponds: a terrain model approach for assessing multiple disturbances at broad
12 scales. *Ecological Applications* **12**:1740-175.
- 13 Griffiths, G. H., J. Lee, and B. C. Eversham. 2000. Landscape pattern and species richness;
14 regional scale analysis from remote sensing. *International Journal of Remote Sensing*
15 **21**:2685-2704.
- 16 Hagen, A. 2003. Fuzzy set approach to assessing similarity of categorical maps. *International*
17 *Journal of Geographical Information Science*. **17**: 235-249.
- 18 Hammond, T. O., and D. L. Verbyla. 1996. Optimistic bias in classification accuracy assessment.
19 *International Journal of Remote Sensing* **17**:1261-1266.
- 20 Hess, G. 1994. Pattern and error in landscape ecology: A commentary. *Landscape Ecology* **9**:35.
- 21 Hess, G. R., and J. M. Bay. 1997. Generating confidence intervals for composition-based
22 landscape indexes. *Landscape Ecology* **12**:309-320
- 23 Imbernon, J., and A. Branthomme. 2001. Characterization of landscape patterns of deforestation

- 1 in tropical rain forests. *International Journal of Remote Sensing* **22**:1753-1765.
- 2 Laurance, W. et al. 2000. Rainforest fragmentation kills big trees. *Nature* **404**: 836.
- 3 McGarigal, K., S. A. Cushman, M. C. Neel, and E. Ene. 2002. FRAGSTATS: Spatial Pattern
4 Analysis Program for Categorical Maps. Computer software program produced by the
5 authors at the University of Massachusetts, Amherst. Available at the following web site:
6 www.umass.edu/landeco/research/fragstats/fragstats.html
- 7 Peralta, P., and P. Mather. 2000. An analysis of deforestation patterns in the extractive reserves
8 of Acre, Amazonia from satellite imagery: a landscape ecological approach. *International*
9 *Journal of Remote Sensing* **21**:2555-2570.
- 10 Plourde, L., and R. G. Congalton. 2003. Sampling method and placement: how do they affect the
11 accuracy of remotely sensed maps? *Photogrammetric Engineering and Remote Sensing*
12 **69**:289-298.
- 13 Pontius, G., Huffaker, D., and K. Denman. 2004. Useful techniques of validation for spatially
14 explicit land-change models. *Ecological Modelling*. **179**: 445-461.
- 15 Rommel, T.K., F. Csillag, S.W. Mitchell, and B. Boots. 2002. Empirical distributions of
16 landscape pattern indices as functions of classified image composition and spatial
17 structure. *Proceedings of Symposium on Geospatial Theory, Processing and*
18 *Applications, Ottawa 2002.*
- 19 Saunders, D.A, Hobbs, R.J., and C.R. Margules. 1991. Biological consequences of ecosystem
20 fragmentation - a review. *Conservation Biology* 5(1): 18-32.
- 21 Saura, S., and J. Martinez-Millan. 2001. Sensitivity of Landscape Pattern metrics to Map Spatial
22 Extent. *Photogrammetric Engineering and Remote Sensing* **67**:1027-1036.
- 23 Shao, G., D. Liu, and G. Zhao. 2001. Relationships of Image Classification Accuracy and

- 1 Variation of Landscape Statistics. *Canadian Journal of Remote Sensing* **27**:33-43.
- 2 Skole, D., and Tucker, C. 1993. Tropical Deforestation and Habitat Fragmentation in the
3 Amazon: Satellite Data from 1978 to 1988. *Science* **260**:1905-1910.
- 4 Stehman, S. V. 2001. Statistical Rigor and Practical Utility in Thematic Map Accuracy
5 Assessment. *Photogrammetric Engineering and Remote Sensing* **67**:727-734.
- 6 Stehman, S. V., J. D. Wickham, J. H. Smith, and L. Yang. 2003. Thematic accuracy of the 1992
7 National Land-Cover Data for the eastern United States: Statistical methodology and
8 regional results. *Remote Sensing of Environment* **86**:500-516.
- 9 Terborgh, J. et al. 2001. Ecological Meltdown in Predator-Free Forest Fragments. *Science* **294**:
10 1923-1926.
- 11 Turner, M.G., R.H. Gardner, and R.V. O'Neill. 2001. *Landscape ecology in theory and practice:*
12 *pattern and process.* Springer-Verlag, New York, New York, USA.
- 13 Turner, M. G., R. V. O'Neill, R. H. Gardner, and B. T. Milne. 1989. Effects of changing spatial
14 scale on the analysis of landscape pattern. *Landscape Ecology* **3**:153-162.
- 15 Villard, M.-A., M. K. Trzcinski, and G. Merriam. 1999. Fragmentation Effects on Forest Birds:
16 Relative Influence of Woodland Cover and Configuration on Landscape Occupancy.
17 *Conservation Biology* **13**: 774-783.
- 18 Wickham, J. D., R. V. O'Neill, K. H. Riitters, T. G. Wade, and K. B. Jones. 1997. Sensitivity of
19 Selected Landscape Pattern metrics to Land-Cover Misclassification in Land-Cover
20 Composition. *Photogrammetric Engineering and Remote Sensing* **63**:397-402.
- 21 WISCLAND (The Wisconsin Initiative for Statewide Cooperation on Landscape Analysis and
22 Data) Land Cover Grid. 1993. User's Guide to WISCLAND Land Cover Data.
23 Wisconsin Department of Natural Resources.

1 With, K. A., and A. W. King. 1997. The use and misuse of neutral landscape models in
2 ecology. *Oikos* **79**:219-229.

3 **FIGURES**

4 Figure 1. Examples of simulated 'correct' landscapes. Landscapes were designed to represent a
5 range of landscape structural features: 3 levels of proportion (20%, 40%, 60% remaining habitat)
6 are shown with varying levels of spatial auto-correlation ($H = 0.2, 0.5, 0.8$). Habitat is shown in
7 white, non-habitat background in black. These nine proportions were used in this study, with 3
8 levels of autocorrelation, and 10 replicates of each scenario for a total of 270 correct maps.

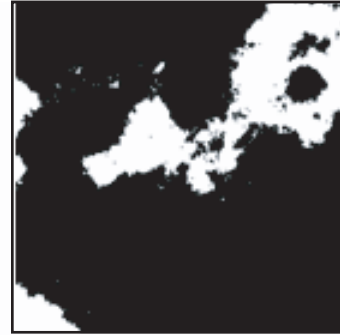
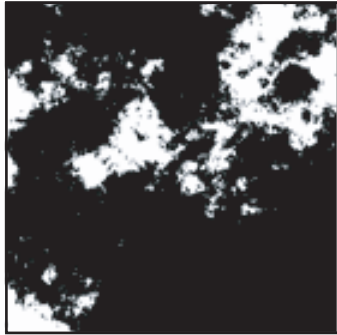
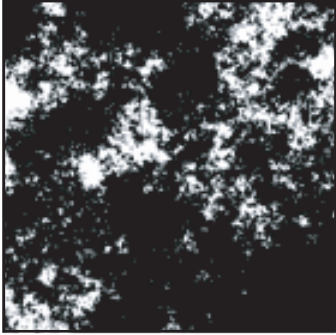
9 Figure 2. Examples of simulated classification errors and smoothing. In this example, a correct
10 landscape is shown (40% habitat, $H=0.5$) at the top. The 'incorrect' map is derived from the
11 correct map but with simulated classification errors of 20% at patch edges and 10% in patch
12 interiors. Smoothing to remove salt-and-pepper error is shown for 3 minimum mapping units
13 (MMU = 2, 4, and 9) whereby all patches smaller than the MMU are reverted to the class of the
14 matrix surrounding the patch.

15 Figure 3. User's error vs. producer's error for the Incorrect and Smoothed landscapes at different
16 MMUs. Top panel shows relationship with habitat proportions labeled and grouped into low (10-
17 30%) medium (40%-60%) and high (70-90%) levels. Bottom panel shows the same data points
18 labeled with the 3 levels of spatial auto-correlation (see Figure 1b for details). Points on
19 smoothed landscapes are labeled according to the H level of the corresponding original correct
20 landscape. Horizontal and vertical lines on the plots mark 15% user's error and producer's error
21 respectively. Figures 4 and 5 only show results from inside this 15% region.

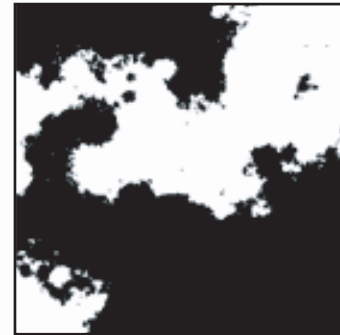
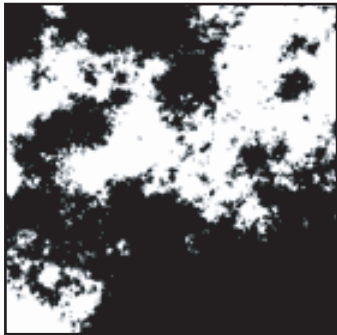
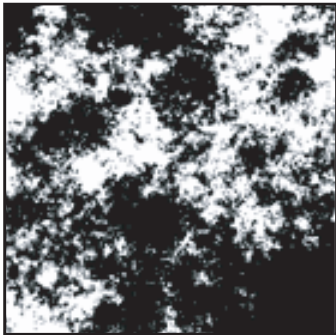
22 Figure 4. Values of raw LPIs on Correct base maps vs. Incorrect and Smoothed landscapes
23 resulting from pattern analysis using Fragstats. Each graph shows one point for each map that

1 had no more than 15% user's error and producer's error. The x axis shows the measured raw
2 LPI value and the y axis shows the correct raw LPI value that the measured value should predict.
3 There are 3 rays on each plot. The central one shows the line that would result if there was no
4 LPI error, that is, correct=measured. The other two rays show errors of +15% and -15% of the
5 correct value for reference. (a-d) Mean Patch Shape, (e-h) Total Edge, (i-l) Number of Patches,
6 (m-p) Mean Patch Size

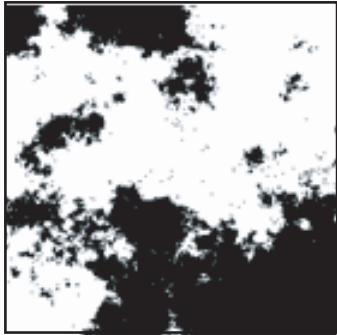
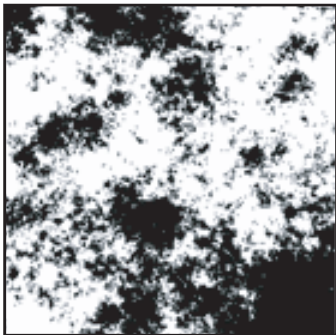
7 Figure 5. Percent LPI Error Relative to the LPI Value for the Correct landscape for four LPIs.
8 Each graph shows one point for each map that had no more than 15% user's error and producer's
9 error. The x axis shows the user's error and the y axis shows the percent error in the LPI. There
10 are 3 lines on each plot. The central line marks the line of no LPI error. As in Figure 4, the other
11 two lines show the boundaries of the interval of LPI errors between +15% and -15% for
12 reference. Points are shaded according to the H value of the corresponding original correct map.
13 (a-d) Mean Patch Shape, (e-h) Total Edge, (i-l) Number of Patches, (m-p) Mean Patch Size



20%
Habitat



40%
Habitat

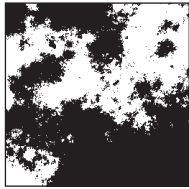


60%
Habitat

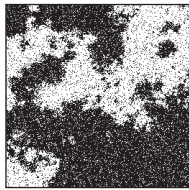
Fragmented
H=0.2

H=0.5

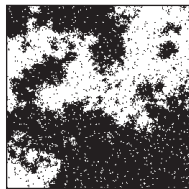
Clumpy
H=0.8



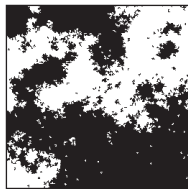
Correct



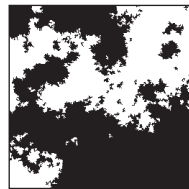
Incorrect



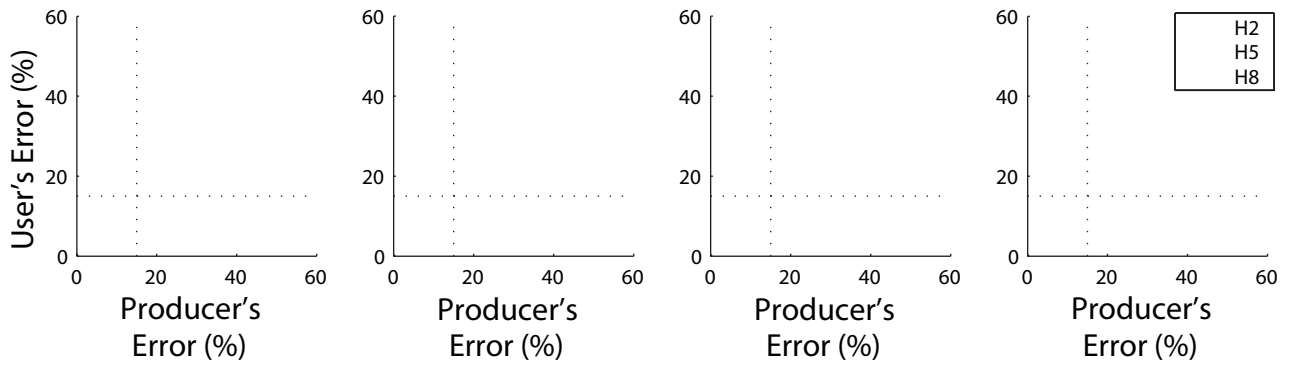
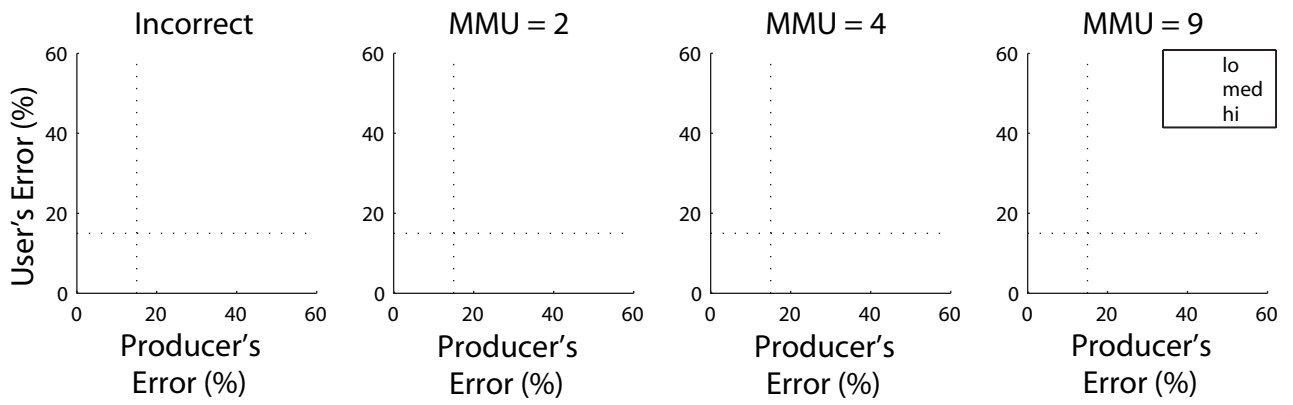
Smoothed
MMU 2

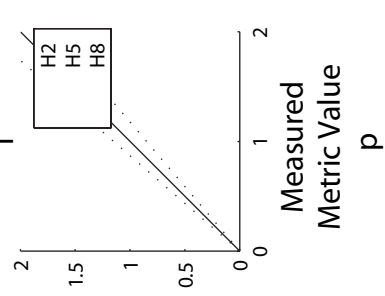
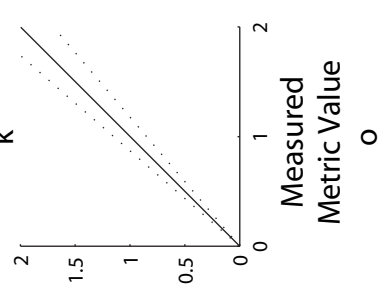
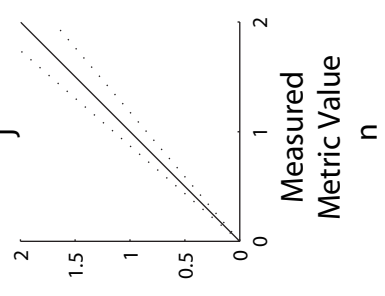
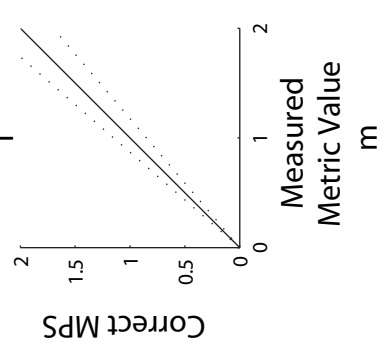
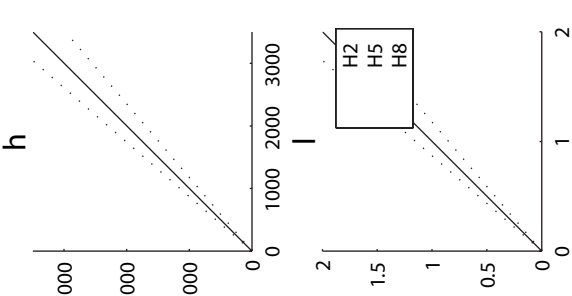
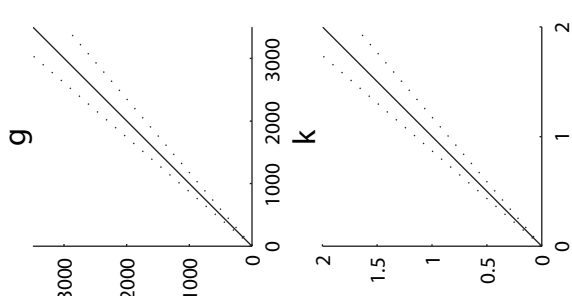
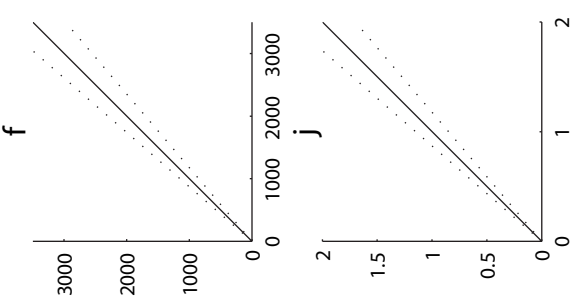
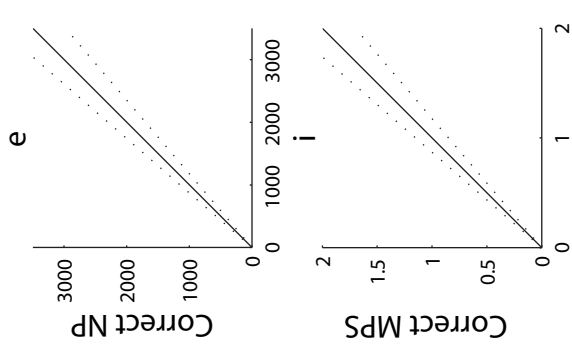
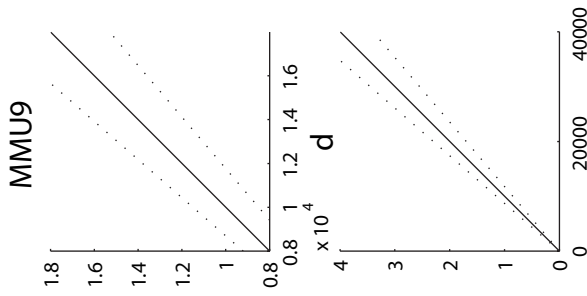
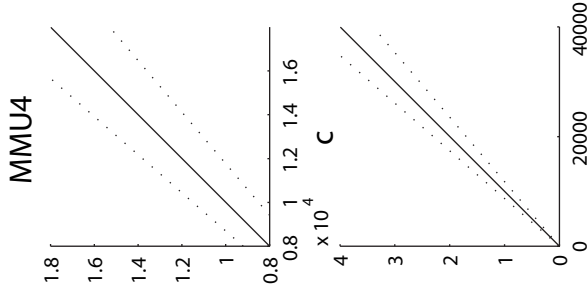
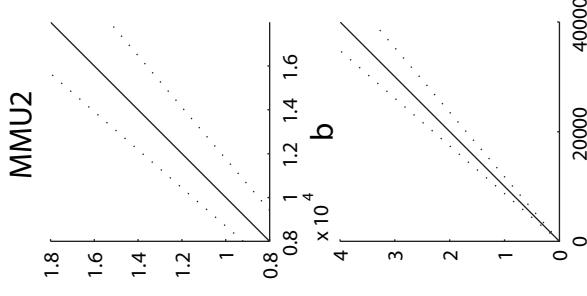
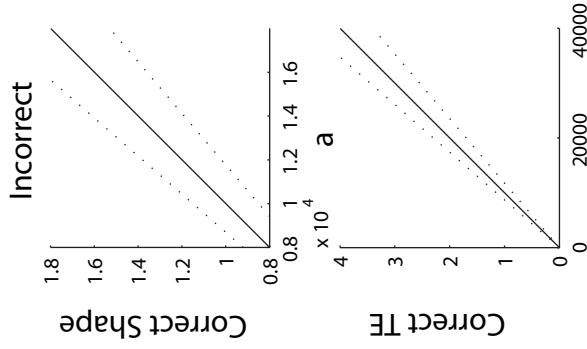


Smoothed
MMU 4



Smoothed
MMU 9





Measured Metric Value
m

Measured Metric Value
n

Measured Metric Value
o

Measured Metric Value
p

